

**CONPASU-tool:**  
**A Concurrent Process Analysis Support tool**  
**based on Symbolic Computation**

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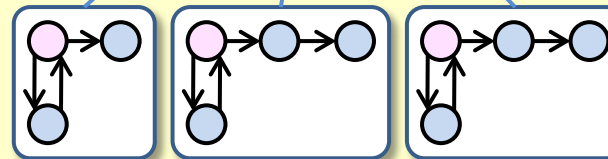
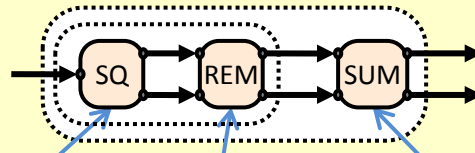
## ■ Summary

CONPASU is a **static analysis** tool of concurrent processes.

### Design

Structures of concurrent processes,  
Behaviors of component processes

#### Structure



#### Behavior

Formalizing

CSP model  
(CSP<sub>M</sub> Script)

Input

### Analysis-results

Feedback



Output

CONPASU

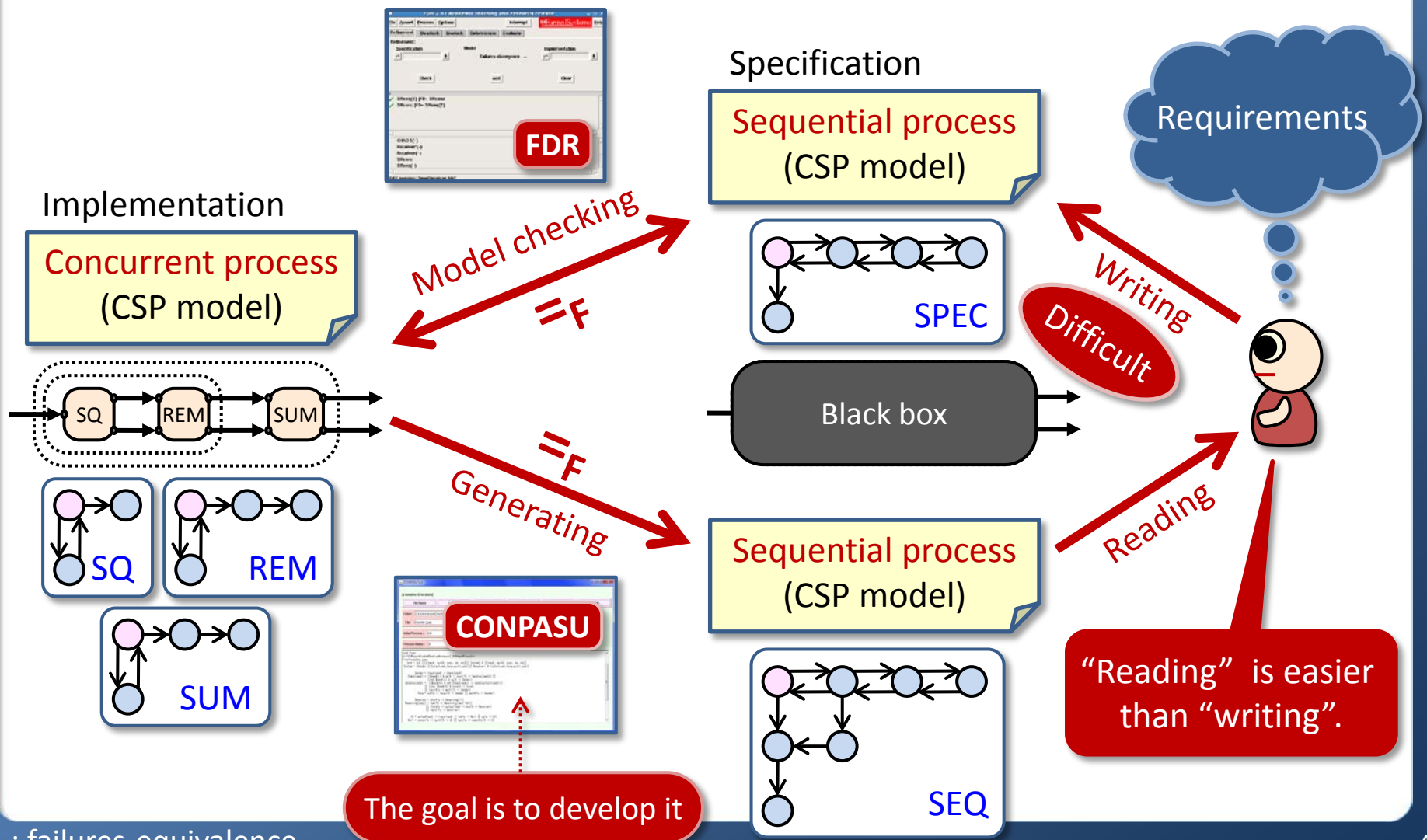
Static analysis

# Introduction

- Motivation
- CONPASU

# Motivation

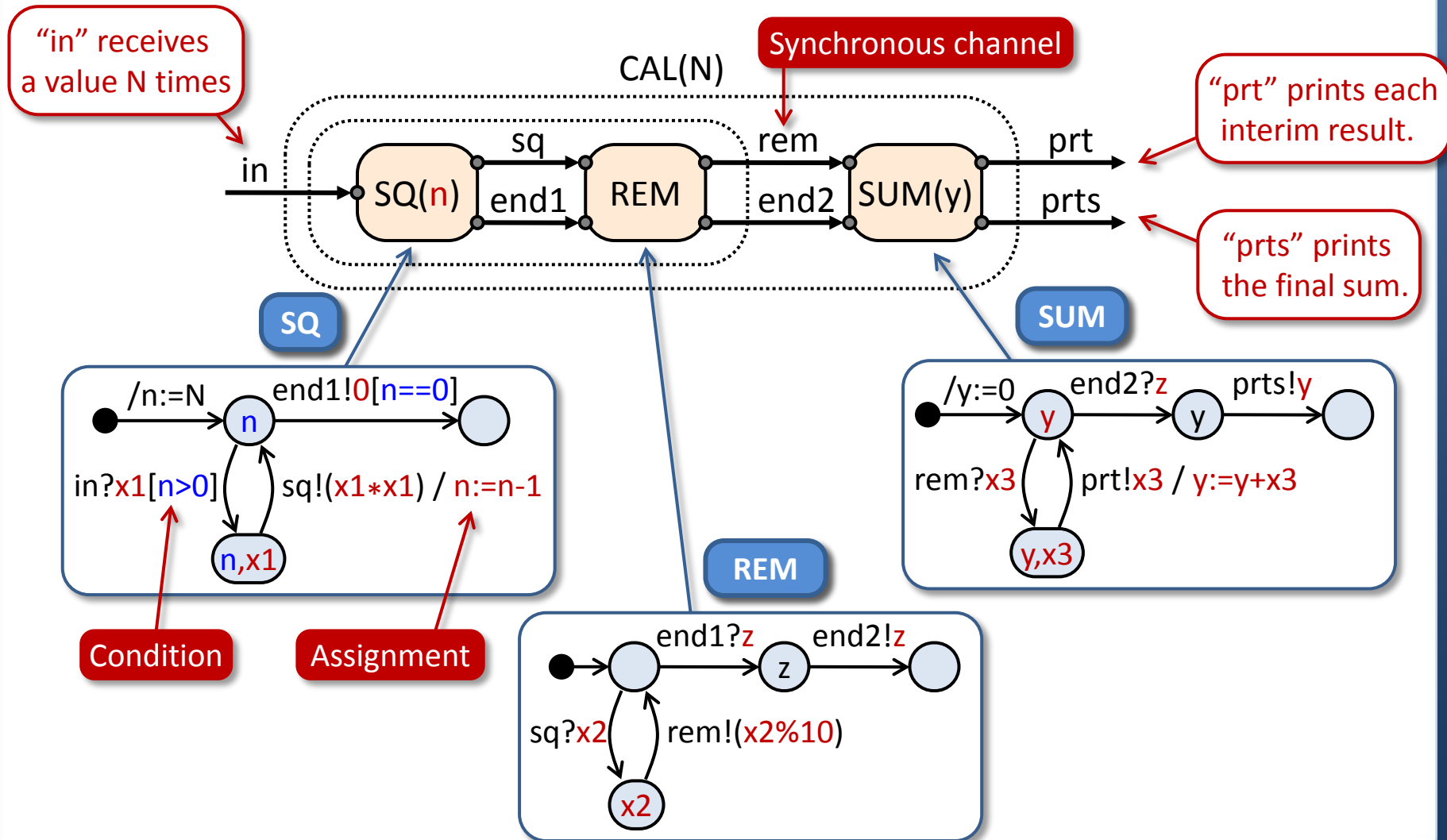
- How can we see behaviors of concurrent processes?



$=_F$  : failures-equivalence

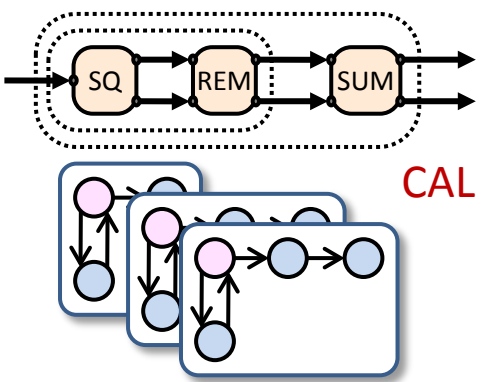
# CAL: An example of concurrent process

- **CAL**: a concurrent process which consists of 3 processes with synchronous channels



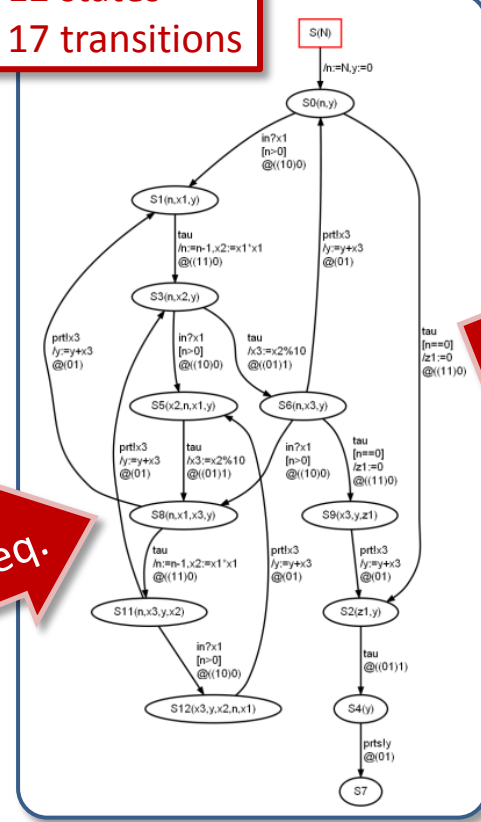
# The analysis method of CONPASU (outline)

- [step 1] A transition graph is generated from a given CSP model (**sequentialization**).
- [step 2] Needless internal-transitions are bypassed (**state-reduction**).

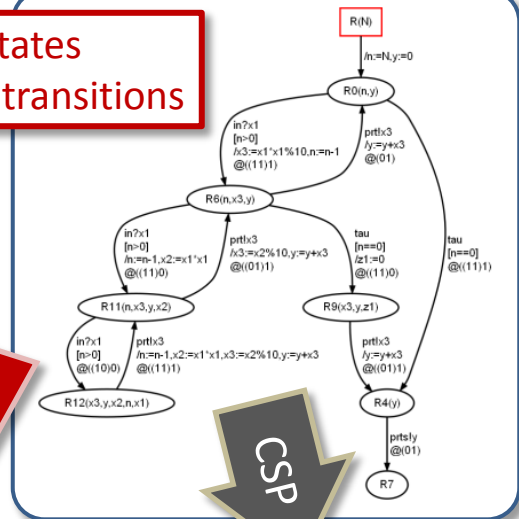


CAL

12 states  
17 transitions



7 states  
10 transitions



Red.

CSP

**Structure**

$$CAL(N) = (SQREM(N) [ \{ \{ rem, end2 \} \} ] SUM(0)) \setminus \{ \{ rem, end2 \} \}$$

$$SQREM(n) = (SQ(n) [ \{ \{ sq, end1 \} \} ] REM) \setminus \{ \{ sq, end1 \} \}$$

**Behavior**

$$SQ(n) = ((n>0) \ \& \ in?x1 \ \rightarrow \ sq!(x1*x1) \ \rightarrow \ SQ(n-1)) \ [ \ [ \ (n=0) \ \& \ end1!0 \ \rightarrow \ STOP \ ] \ ]$$

$$REM = sq?x2 \ \rightarrow \ rem!(x2\%10) \ \rightarrow \ REM \ [ \ [ \ end1?z1 \ \rightarrow \ end2!z1 \ \rightarrow \ STOP \ ] \ ]$$

$$SUM(y) = rem?x3 \ \rightarrow \ prt!x3 \ \rightarrow \ SUM(y+x3) \ [ \ [ \ end2?z2 \ \rightarrow \ prts!y \ \rightarrow \ STOP \ ] \ ]$$

**Concurrent process (CSP model)**

Seq.

$$SEQ(N) = SEQ0(N,0) \setminus \{ \{ tmp \} \}$$

$$SEQ0(n,y) = (n>0) \ \& \ in?x1 \ \rightarrow \ SEQ6(n-1,x1*x1\%10,y) \ [ \ [ \ (n=0) \ \& \ tmp!0 \ \rightarrow \ SEQ4(y) \ ] \ ]$$

$$SEQ4(y) = prts!(y) \ \rightarrow \ SEQ7$$

$$SEQ6(n,x3,y) = (n>0) \ \& \ in?x1 \ \rightarrow \ SEQ11(n-1,x3,y,x1*x1) \ [ \ [ \ (n=0) \ \& \ tmp!0 \ \rightarrow \ SEQ9(x3,y,0) \ ] \ ] \ [ \ [ \ prt!(x3) \ \rightarrow \ SEQ0(n,y+x3) \ ] \ ]$$

$$SEQ7 = STOP$$

$$SEQ9(x3,y,z1) = prt!(x3) \ \rightarrow \ SEQ4(y+x3)$$

$$SEQ11(n,x3,y,x2) = (n>0) \ \& \ in?x1 \ \rightarrow \ SEQ12(x3,y,x2,n,x1) \ [ \ [ \ prt!(x3) \ \rightarrow \ SEQ6(n,x2\%10,y+x3) \ ] \ ]$$

$$SEQ12(x3,y,x2,n,x1) = prt!(x3) \ \rightarrow \ SEQ11(n-1,x2\%10,y+x3,x1*x1)$$

**Sequential process (CSP model)**



=<sub>F</sub> : (stable) failures-equivalence

# Analysis method

- Sequentialization
- State-reduction
- Abstraction

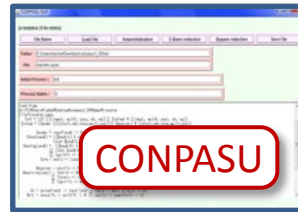
# Sequentialization

- A **symbolic** operational semantics with data-assignments and **locations** is used.
- Variables are **not instantiated** to values in **symbolic** semantics.
  - Many values can be folded into a variable in symbolic labeled transition graphs.
  - State-**minimization** is difficult (often undecidable).

## The CSP model of CAL(N)

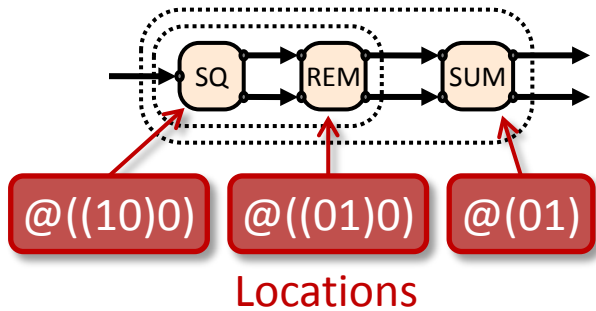
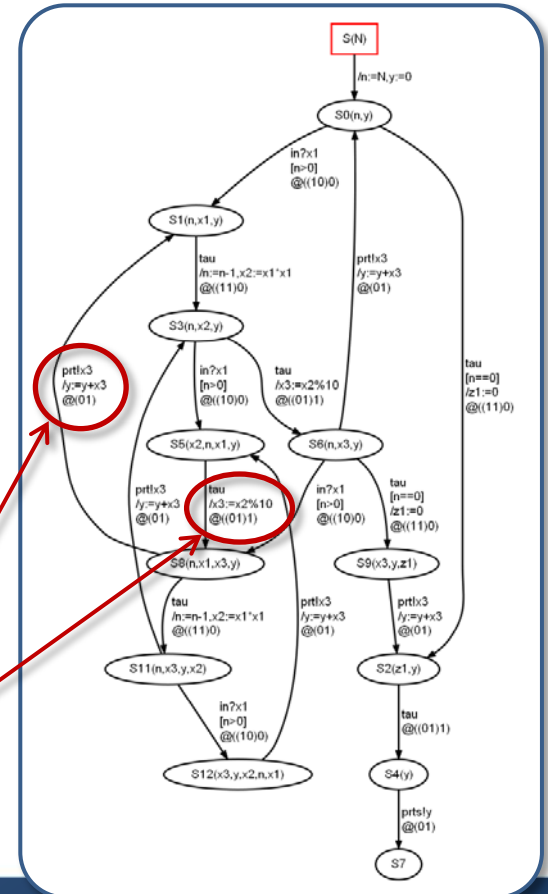
$CAL(N) = (SQREM(N) [| \{ \{ rem, end2 \} \} ] ] SUM(0)) \not\equiv \{ \{ rem, end2 \} \}$   
 $SQREM(n) = (SQ(n) [| \{ \{ sq, end1 \} \} ] ] REM) \not\equiv \{ \{ sq, end1 \} \}$

$SQ(n) = ((n > 0) \& in?x1 \rightarrow sq!(x1 * x1) \rightarrow SQ(n-1))$   
 $[ ] ((n == 0) \& end1!0 \rightarrow STOP)$   
 $REM = sq?x2 \rightarrow rem!(x2 \% 10) \rightarrow REM$   
 $[ ] end1?z1 \rightarrow end2!z1 \rightarrow STOP$   
 $SUM(y) = rem?x3 \rightarrow prt!x3 \rightarrow SUM(y+x3)$   
 $[ ] end2?z2 \rightarrow prts!y \rightarrow STOP$



CONPASU

Symbolic operational semantics



prt!x3 / y:=y+x3 @ (01)

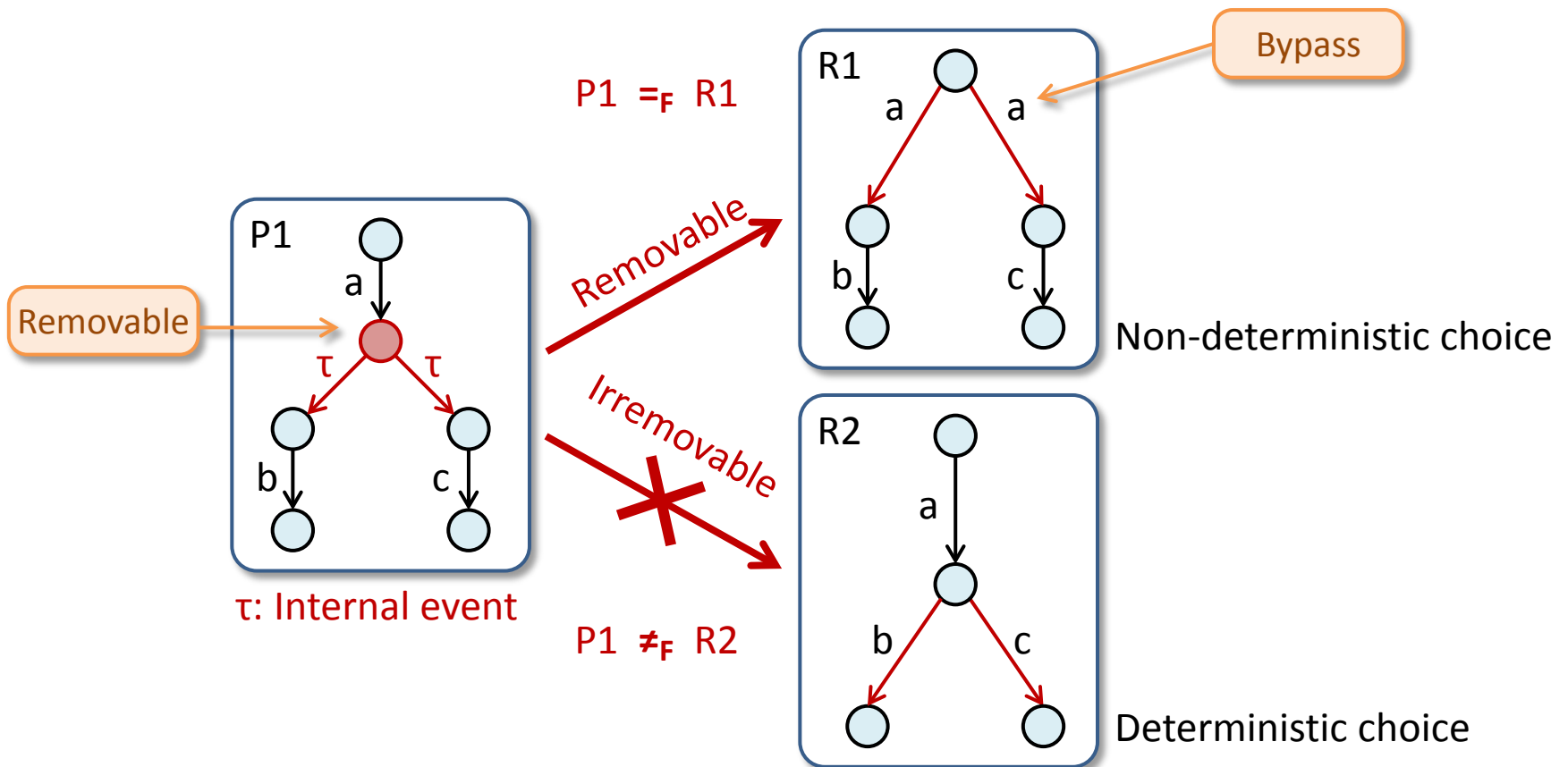
τ / x3:=x2%10 @ ((01)1)

τ: Internal event



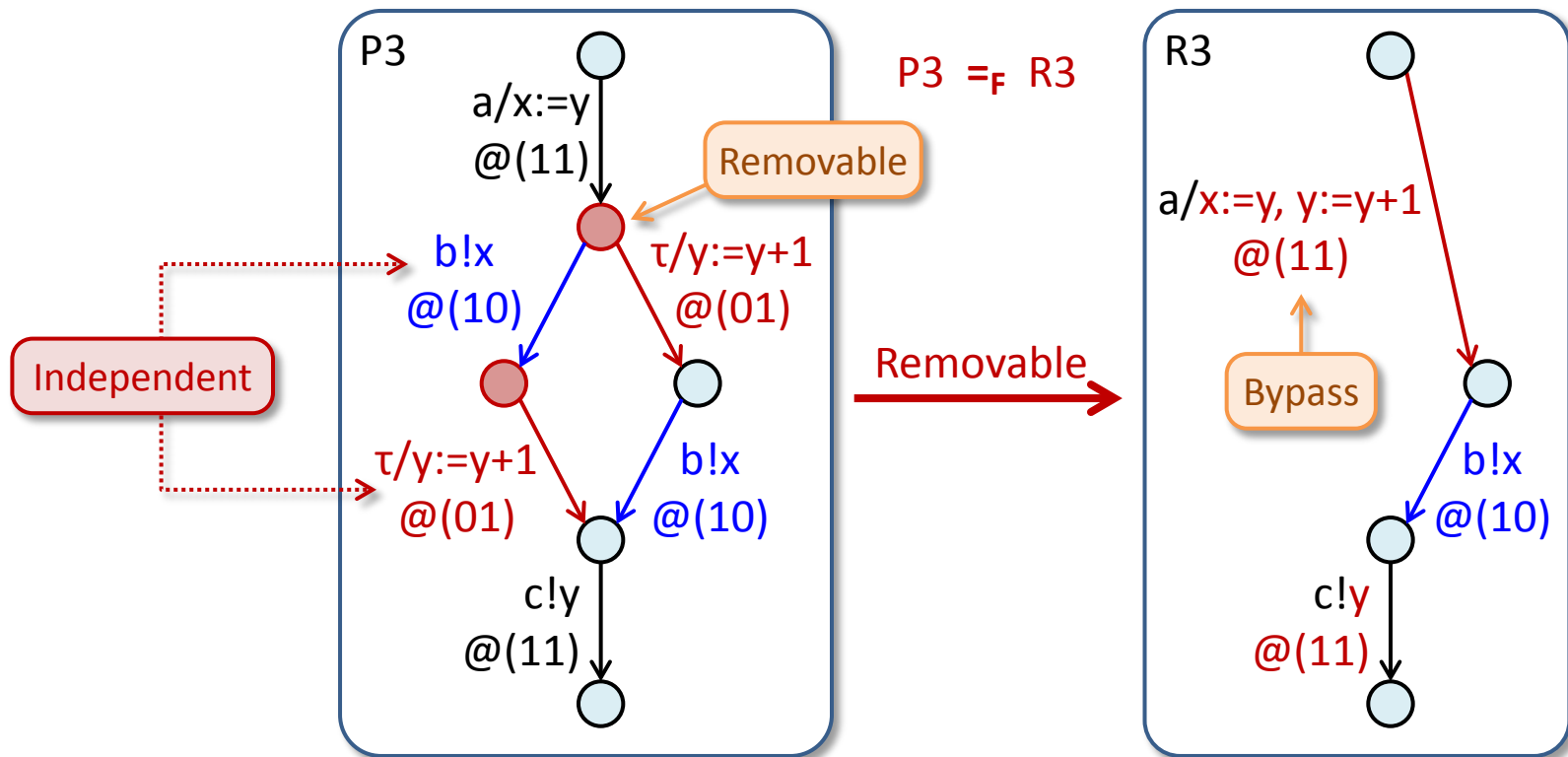
# State-reduction (internal-choice)

- Needless **internal transitions** are bypassed with preserving the **failures-equivalence**  $=_F$ .  
e.g. A removable state with **non-deterministic internal transitions**.  
(in fact, it is more complex because conditions and assignments are considered)



# State-reduction (interleaving)

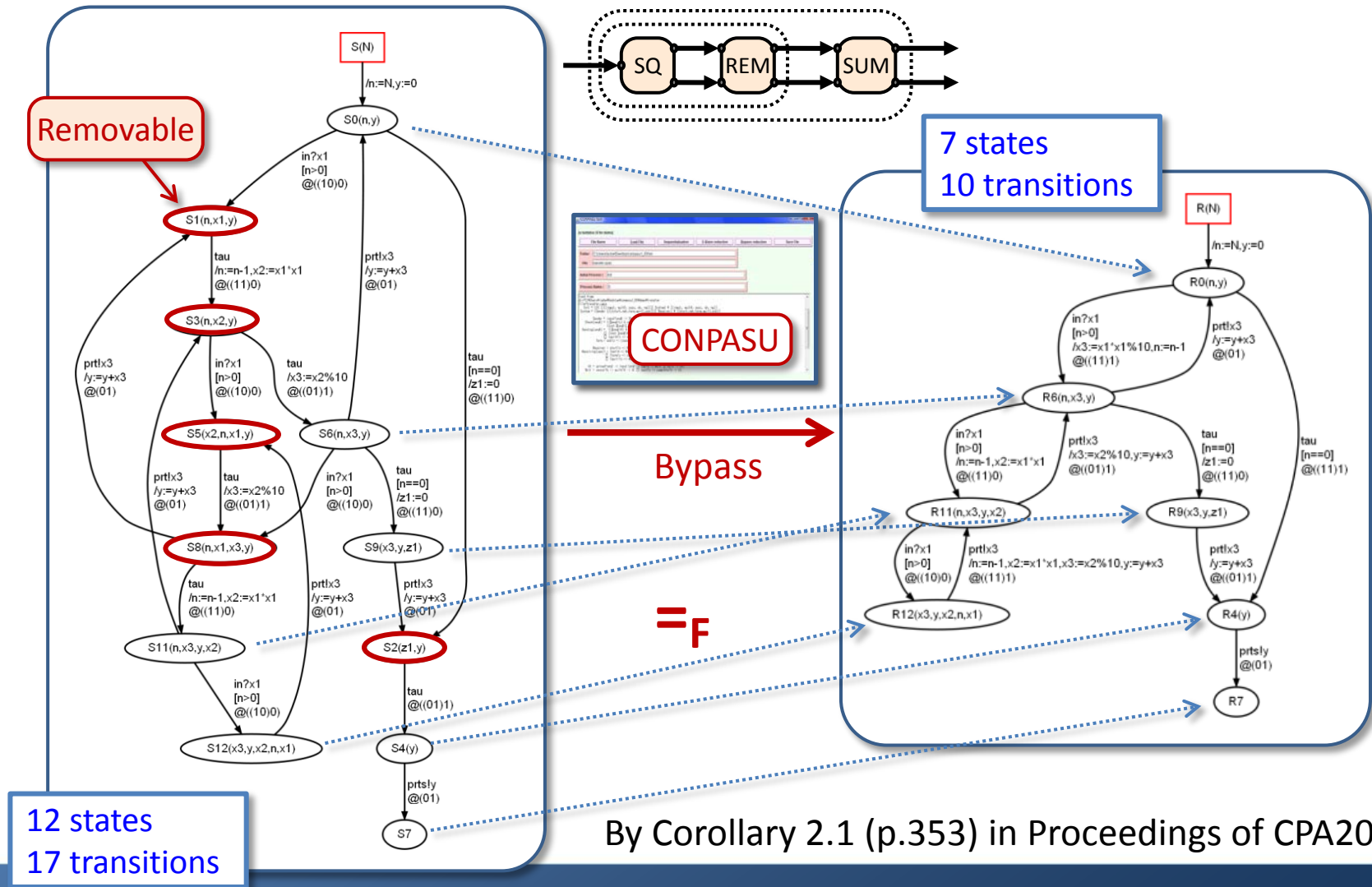
- Needless **internal transitions** are bypassed with preserving **failures-equivalence  $=_F$** .  
e.g. Removable states with **interleaving**.



In CONPASU, locations are used for checking the independency.

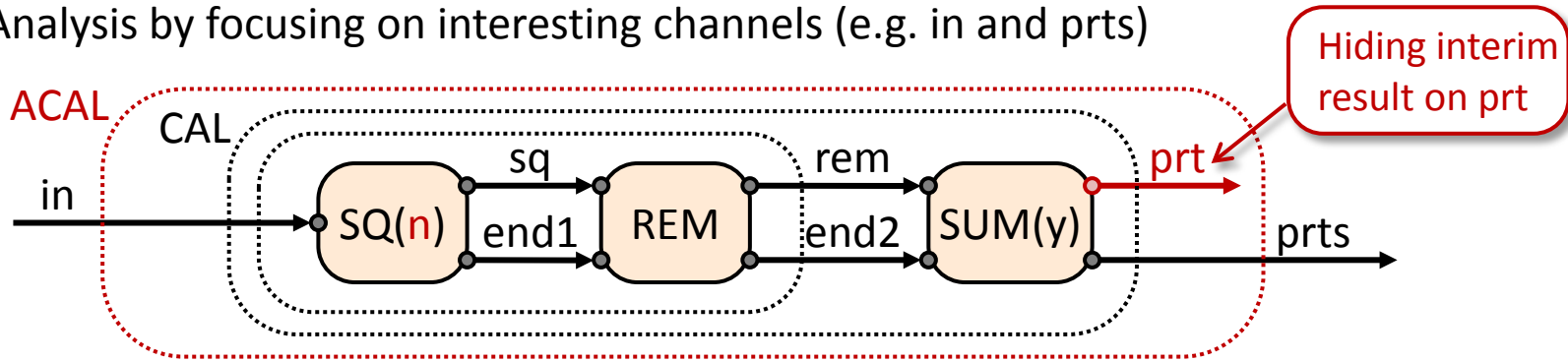
# State-reduction (an example)

- The removable states in the transition graph of  $CAL(N)$  and the reduced graph.

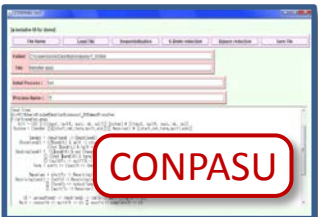


# Abstraction

- Analysis by focusing on interesting channels (e.g. in and prts)

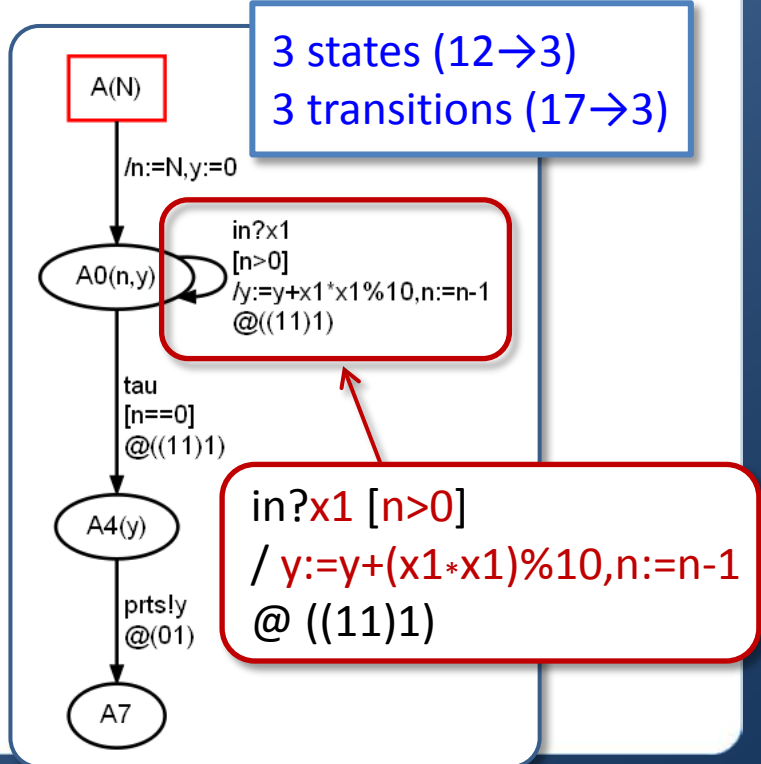


$ACAL(N) = CAL(N) \setminus \{|prt|\}$   
 $CAL(N) = (SQREM(N) [|{|rem,end2|}]) SUM(0) \setminus \{|rem,end2|\}$   
 $SQREM(n) = (SQ(n) [|{|sq,end1|}]) REM \setminus \{|sq,end1|\}$   
 $SQ(n) = ((n>0) \ \& \ in?x1 \ -> \ sq!(x1*x1) \ -> \ SQ(n-1))$   
 $\ [] \ ((n==0) \ \& \ end1!0 \ -> \ STOP)$   
 $REM = sq?x2 \ -> \ rem!(x2\%10) \ -> \ REM$   
 $\ [] \ end1?z1 \ -> \ end2!z1 \ -> \ STOP$   
 $SUM(y) = rem?x3 \ -> \ prt!x3 \ -> \ SUM(y+x3)$   
 $\ [] \ end2?z2 \ -> \ prts!y \ -> \ STOP$



CONPASU

Sequentialization,  
State-reduction



# Application

- Data-sequence transfer
- Analysis

# The CSP model of TransferSys

- TransferSys is a concurrent process that consists of 3 processes: **UI**, **Sender**, and **Receiver**.
- Sender** transfers data-sequences from **UI** to **Receiver** (it can be cancelled).

## The CSP model of TransferSys

### TransferSys

```
TransferSys = (UI [|{|input, quit0, succ, ok, ng|}] Transfer)
              \ {|input, quit0, succ, ok, ng|}

Transfer = (Sender [|{|start, net, term, quit1, ack|}] Receiver)
           \ {|start, net, term, quit1, ack|}
```

Structure

### UI

```
UI = upload?ds -> input!ds -> (ok?a -> Wait [| ng?a -> UI]
                               \ {|input, quit0, succ, ok, ng|})
    Wait = cancel?b -> quit0!0 -> UI [| succ?u -> complete!0 -> UI]
```

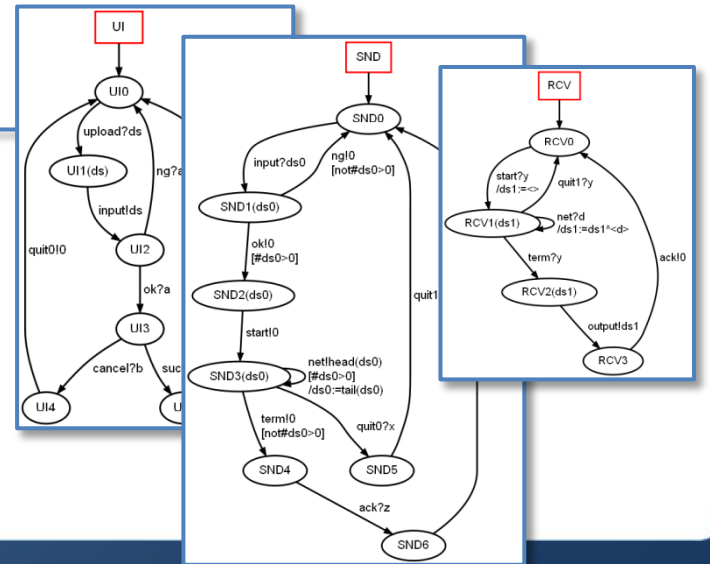
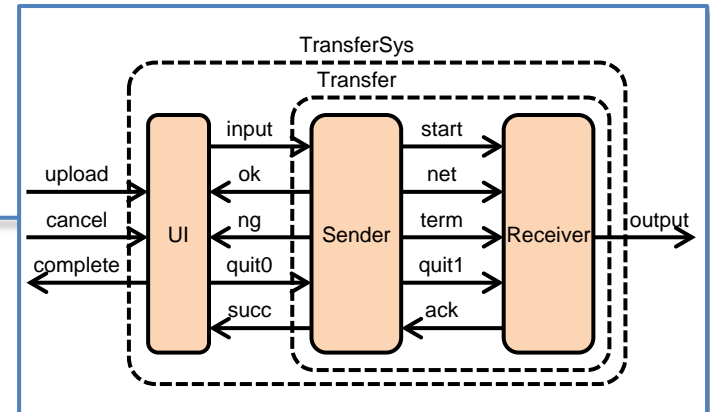
### Sender

```
Sender = input?ds0 -> Check(ds0)
        Check(ds0) = ((#ds0>0) & ok!0 -> start!0 -> Sending(ds0))
                    [| ((not #ds0>0) & ng!0 -> Sender)
                    \ {|input, quit0, succ, ok, ng|}
        Sending(ds0) = ((#ds0>0) & net!(head(ds0)) -> Sending(tail(ds0)))
                       [| ((not #ds0>0) & term!0 -> Term)
                       \ {|start, net, term, quit1, ack|}
                       [| (quit0?x -> quit1!0 -> Sender)
        Term = ack?z -> succ!0 -> Sender
```

### Receiver

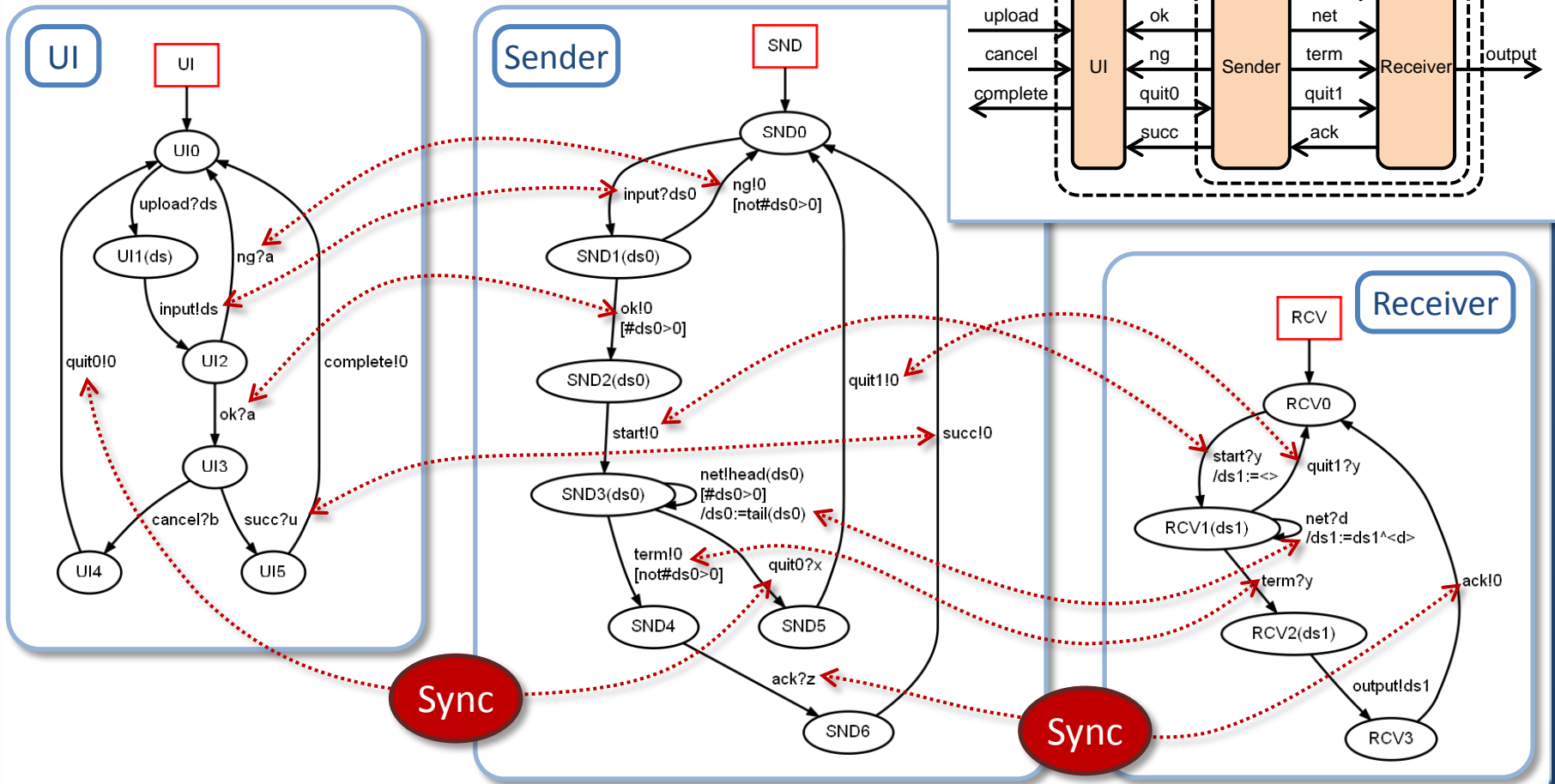
```
Receiver = start?y -> Receiving(<>)
          Receiving(ds1) = (net?d -> Receiving(ds1^<d>))
                           [| (term?y -> output!ds1 -> ack!0 -> Receiver)
                           \ {|start, net, term, quit1, ack|}
                           [| (quit1?y -> Receiver)
```

Behavior



# The behaviors of the 3 components

- Sender **synchronously communicates** with UI or Receiver.  
 → How does **their composition** behave?



# The behavior of TransferSys

ds0 : the sequence-variable in Sender  
 ds1 : the sequence-variable in Receiver

- The symbolic labeled transition graph generated by CONPASU from TransferSys

TransferSys \ {|complete|}

```

TransferSys = (UI [|{input, quit0, succ, ok, ng}|] Transfer)
              \ {|input, quit0, succ, ok, ng|}

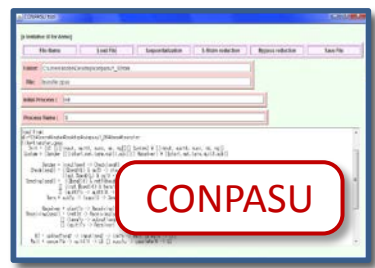
Transfer = (Sender [|{start, net, term, quit1, ack}|] Receiver)
           \ {|start, net, term, quit1, ack|}

UI = upload?ds -> input!ds -> (ok?a -> Wait [] ng?a -> UI)
Wait = cancel?b -> quit0!0 -> UI [] succ?u -> complete!0 -> UI

Sender = input?ds0 -> Check(ds0)
Check(ds0) = ((#ds0>0) & ok!0 -> start!0 -> Sending(ds0))
             [] ((not #ds0>0) & ng!0 -> Sender)
Sending(ds0) = ((#ds0>0) & net!(head(ds0)) -> Sending(tail(ds0)))
              [] ((not #ds0>0) & term!0 -> Term)
              [] (quit0?x -> quit1!0 -> Sender)
Term = ack?z -> succ!0 -> Sender

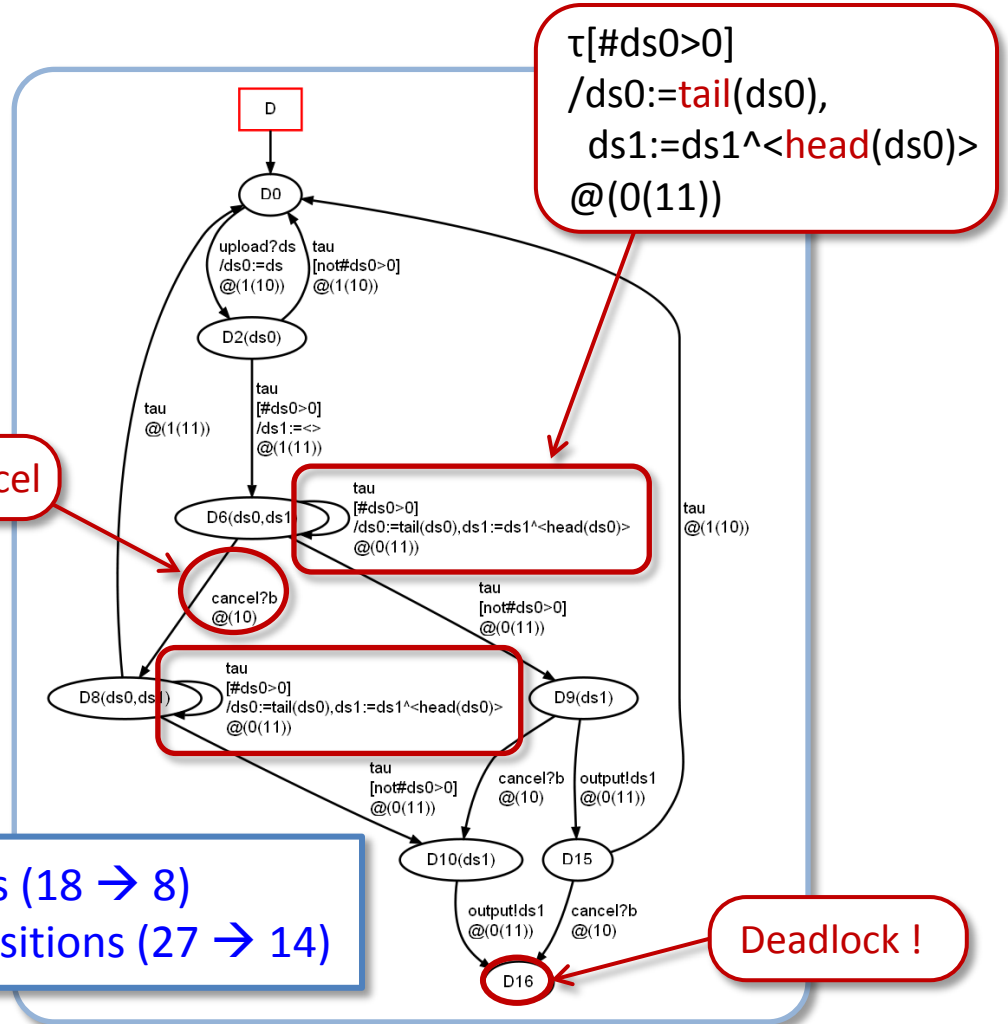
Receiver = start?y -> Receiving(<)
Receiving(ds1) = (net?d -> Receiving(ds1^<d>))
                [] (term?y -> output!ds1 -> ack!0 -> Receiver)
                [] (quit1?y -> Receiver)
    
```

Sequentialization,  
 State-reduction



CONPASU

8 states (18 → 8)  
 14 transitions (27 → 14)



Cancel

$\tau[\#ds0>0]$   
 $/ds0:=tail(ds0),$   
 $ds1:=ds1^<head(ds0)>$   
 $@(0(11))$

$\tau$   
 $[\#ds0>0]$   
 $/ds0:=tail(ds0), ds1:=ds1^<head(ds0)>$   
 $@(0(11))$

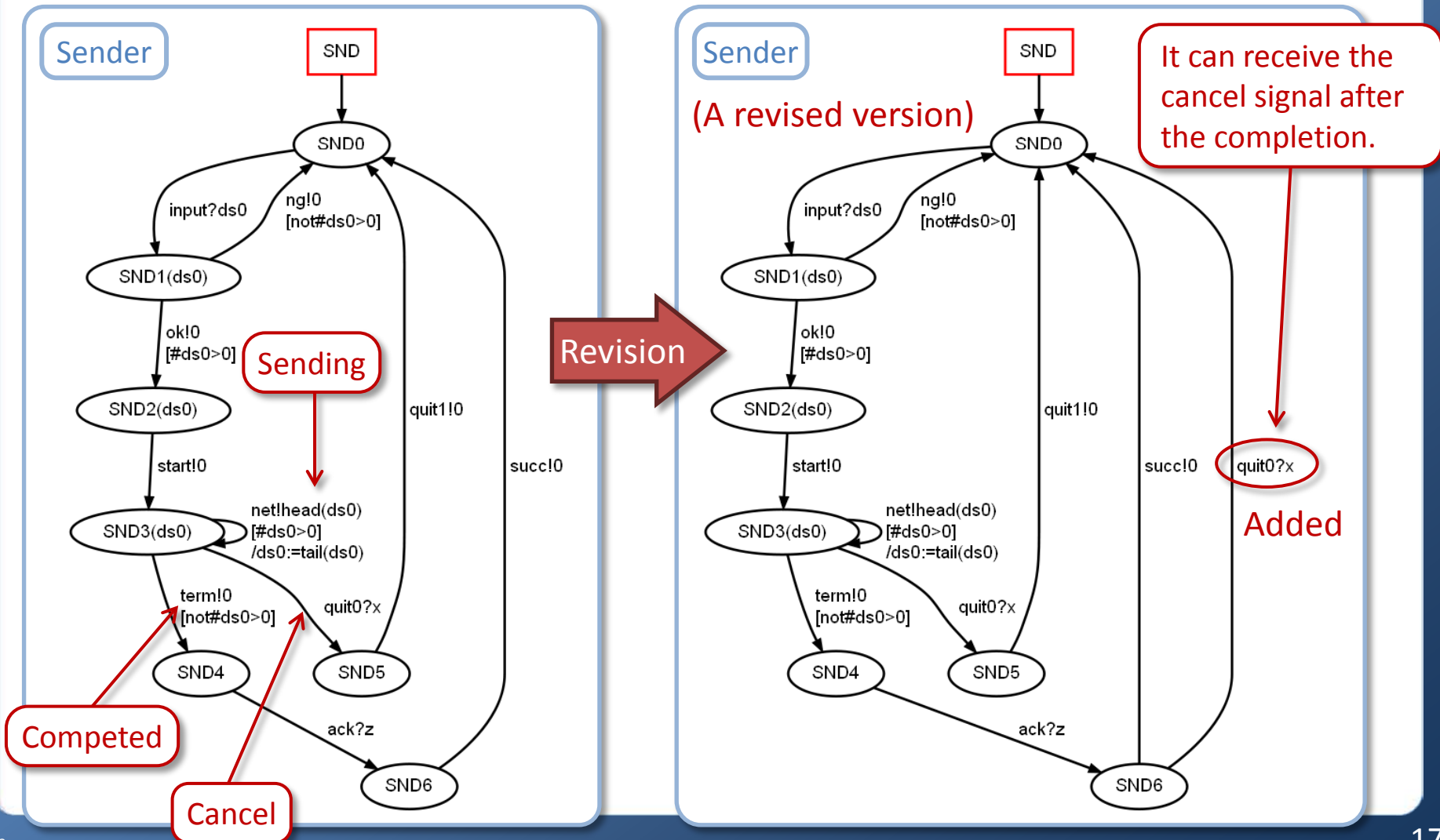
$\tau$   
 $[\#ds0>0]$   
 $/ds0:=tail(ds0), ds1:=ds1^<head(ds0)>$   
 $@(0(11))$

Deadlock !



# A revision of Sender

- A transition is added in Sender for receiving the cancel signal after transfer completion.



# The behavior of the revised TransferSys

- The transition graph of the revised TransferSys.

TransferSys \ {|complete |}

```

TransferSys = (UI [|{|input, quit0, succ, ok, ng |}] Transfer)
              \ {|input, quit0, succ, ok, ng |}

Transfer = (Sender [|{|start, net, term, quit1, ack |}] Receiver)
           \ {|start, net, term, quit1, ack |}

UI = upload?ds -> input!ds -> (ok?a -> Wait [| ng?a -> UI])
Wait = cancel?b -> quit0!0 -> UI [| succ?u -> complete!0 -> UI]

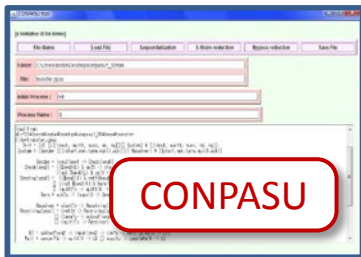
Sender = input?ds0 -> Check(ds0)
Check(ds0) = ((#ds0>0) & ok!0 -> start!0 -> Sending(ds0))
             [| ((not #ds0>0) & ng!0 -> Sender)]
Sending(ds0) = ((#ds0>0) & net!(head(ds0)) -> Sending(tail(ds0)))
              [| ((not #ds0>0) & term!0 -> Term)
               [| (quit0?x -> quit1!0 -> Sender)]

Term = ack?z -> (succ!0 -> Sender [| quit0?x -> Sender])

Receiver = start?y -> Receiving(< >)
Receiving(ds1) = (net?d -> Receiving(ds1^<d ->))
                [| (term?y -> output!ds1 -> ack!0 -> Receiver)
                 [| (quit1?y -> Receiver)]
    
```

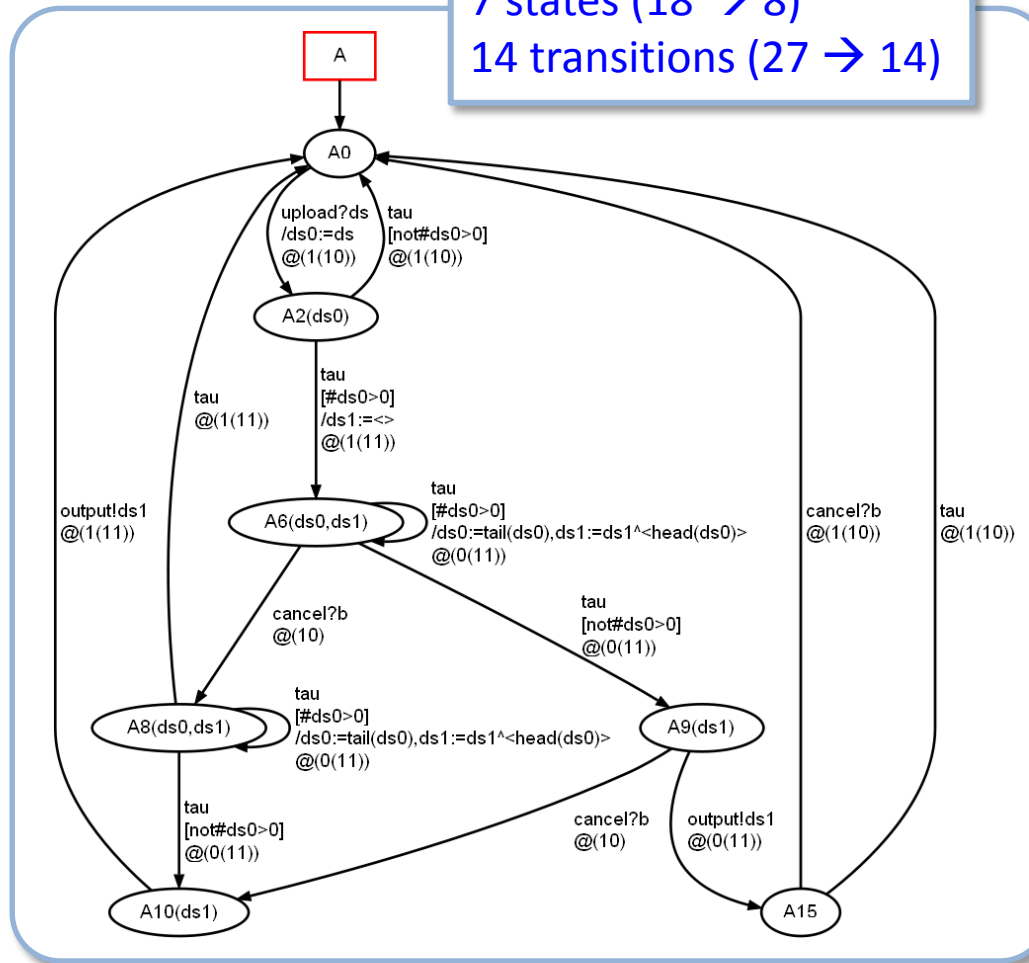
Revised

Sequentialization,  
State-reduction



CONPASU

7 states (18 → 8)  
14 transitions (27 → 14)



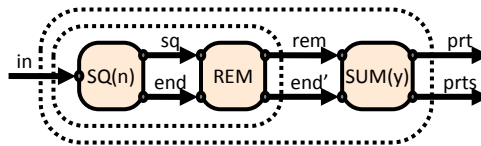
## Related works

- PAT
- LTSA

# PAT (Process Analysis Toolkit)

- PAT can display transition graphs of CSP models.
- Standard (**non-symbolic**) semantics is used. (all variables are **instantiated** to possible values)

CAL



PAT (GUI)

```

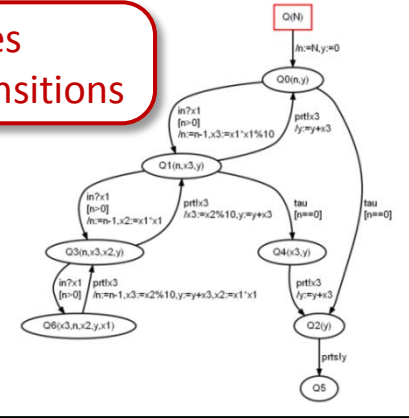
PAT - An Enhanced Simulation and Model Checking Tool (Version 2.9.1)
Specification Check Grammar (F5) Simulation (F6) Verification (F7)
File Edit View Tools Examples Window Help
Document 1 / cal3.csp
5 channel end2 0;
6 channel prt 0;
7 channel prts 0;
8
9 #alphabet SQ {in,sq,end};
10 #alphabet REM {sq,rem,end2};
11 #alphabet SUM {rem,prt,prts,sum};
12
13 CAL = {SQ(3) || REM || SUM(0)}
14 \ {sq.0,sq.1,sq.2,sq.4,sq.9,sq.16,end.0,
15 rem.0,rem.1,rem.2,rem.3,rem.4,rem.6,rem.9,end2.0};
16
17 SQ(c) = if (c>0) (in?x -> sq!(x*x) -> SQ(c-1))
18 [] if (c==0) (end!0 -> Stop);
19
20 REM = sq?x -> rem!(x%10) -> REM
21 [] end?z -> end2!z -> Stop;
22
23 SUM(y) = rem?x -> prt!x -> SUM(y+x)
24 [] end2?z -> prts!y -> Stop;
    
```

by Simulator

fix N=3 and finitize input in {0,1}

cf. CONPASU

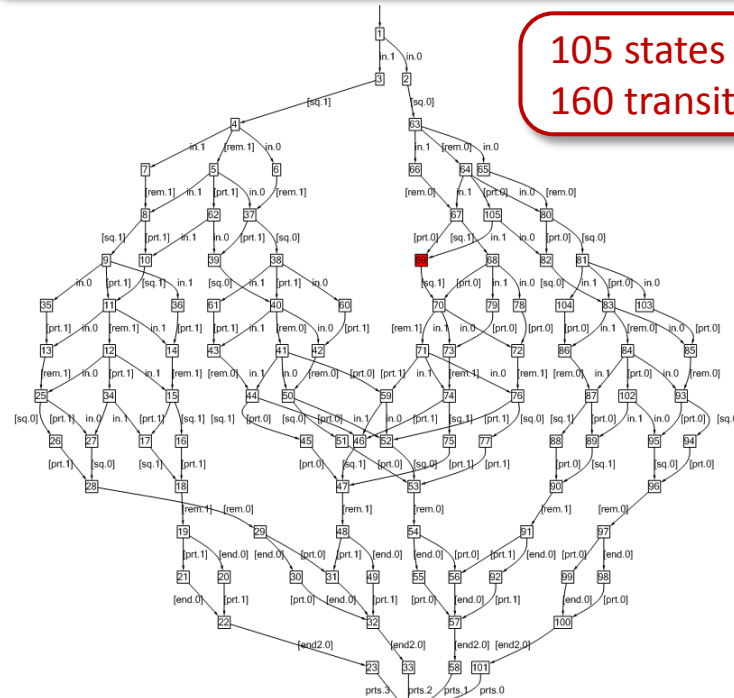
8 states  
12 transitions



any N and any input

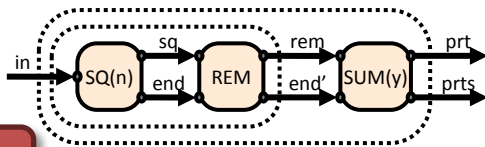
The standard transition graph of CAL(3)

105 states  
160 transitions



# LTSA (LTS analyzer)

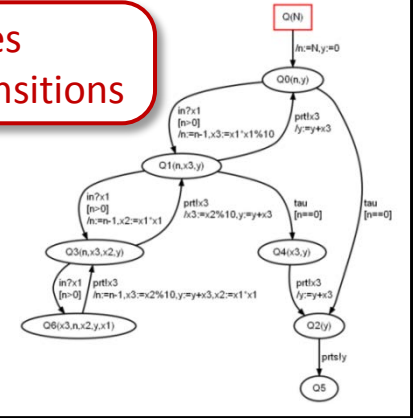
- **LTSA** can display **minimized** transition graphs.
- Standard (**non-symbolic**) semantics is used.  
(all variables are **instantiated** to possible values)



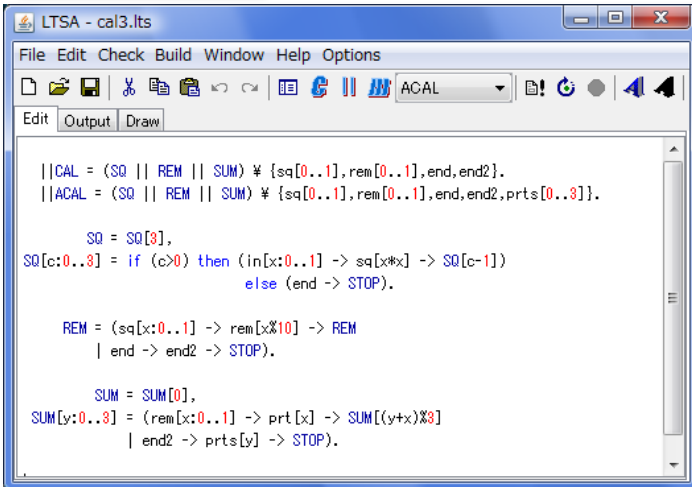
any N and any input

cf. CONPASU

8 states  
12 transitions



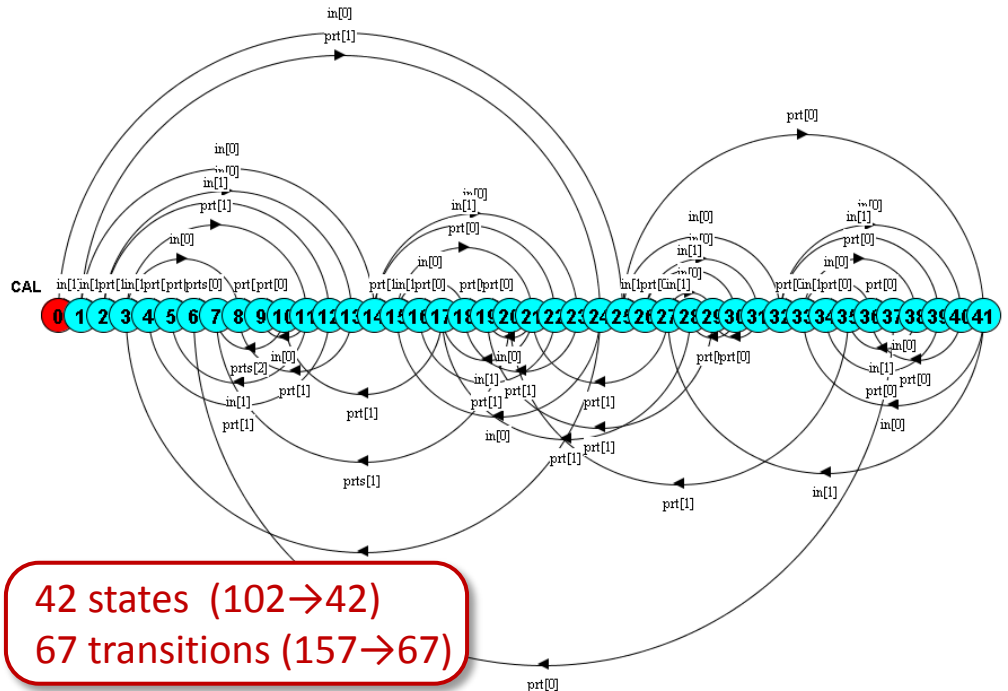
LTSA (GUI)



by Draw

fix N=3 and finitize input in {0,1}

The minimized standard transition graph of CAL(3)



42 states (102→42)  
67 transitions (157→67)

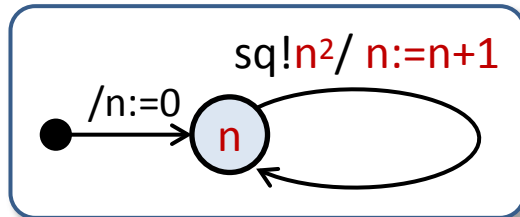
# Summary

- Advantages
- Future works

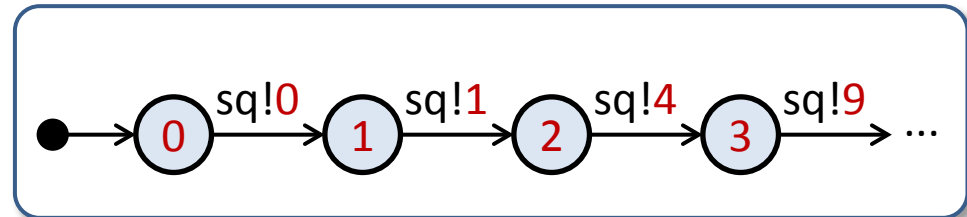
# Summary

- A **symbolic analysis method** and its **implementation** CONPASU have been presented.
  - The **advantages[A]** and **disadvantages[D]** of CONPASU compared with model-checkers:
    - [A] Symbolic operational semantics is used (i.e. variables are **not instantiated**),
    - [A] An equal sequential process (and the graph) can be **automatically generated**.
    - [D] Symbolic labels are usually **more complex** than standard (instantiated) labels.
    - [D] Generated sequential processes are **not necessarily optimized** (e.g. not minimized).
- CONPASU and model checker will **complement** each other.

By symbolic semantics



By standard (non-symbolic) semantics



$$S(n) = \text{sq!}n^2 \rightarrow S(n+1)$$

## Future works:

- Careful consideration about **livelocks**
- Symbolic computation of **data-expressions** ( $1+2 \neq 2+1$  in the prototype)
- Improvement of CONPASU (Java, 6,000 lines) and evaluation of **performance**