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Development of an ML-based Verification Tool for Timed CSP Processes

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Activity of Our group (TMU)

- Development of TPCORE (IP core of general purpose processor) (CPA2004)
 - compatible with transputer assembly language
 - Programs written in (Inmos) occam can be executed
 - 50MHz (FPGA) and 130MHz (ASIC)
- TPCORE2 (one of 4 link I/Fs→DS-link for virtual link and IEEE1355), 1355 router (PDNS2010) and FPU
- Application of these processors in embedded system
 - Real time programming
 - Need a Timed CSP verification tool ← **Motivation for this study**

CSP and Timed CSP

- CSP: Process transition with events only (event transition)

$$P \xrightarrow{\mu} P'$$

- Timed CSP: Consideration of process transition with time (evolution transition)

$$Q \xrightarrow{t} Q'$$

New Operators for Timed CSP(1)

- Timed Event Prefix $a@u \longrightarrow P$

Occurrence time of event a after start of the process is recorded in timed variable u . Once a is occurred, P can refer the value recorded in u .

$$(a@u \rightarrow P) \xrightarrow{a} P[0/u]$$

Reset u at event a

$$(a@u \rightarrow P) \overset{d}{\rightsquigarrow} (a@u \rightarrow P[u + d/u])$$

a is not occurred after time d has passed

$$(a@u \rightarrow out!u \rightarrow SKIP) \overset{5}{\rightsquigarrow}$$

$$(a@u \rightarrow out!(u + 5) \rightarrow SKIP) \xrightarrow{a}$$

$$(out!(0 + 5) \rightarrow SKIP) \xrightarrow{out.5} SKIP$$

New Operators for Timed CSP(2)

- Timeout $P \triangleright^d Q$
Choice with an event in P and the elapsed time from start of the process;
for example,

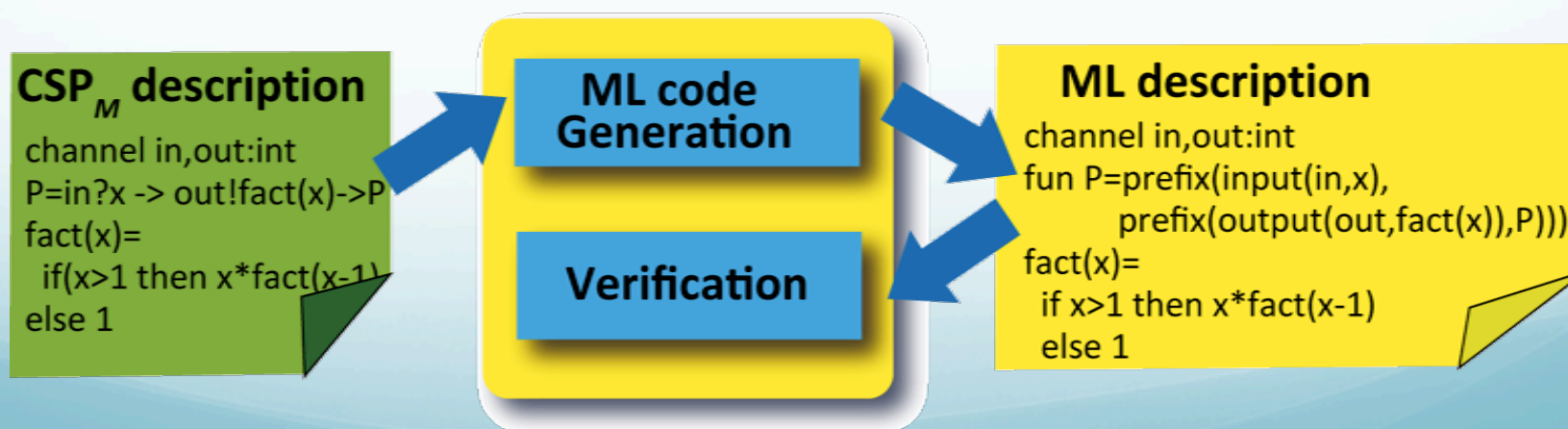
$$(a \rightarrow P) \triangleright^d Q$$

the process P will follow after the event a if a takes place in d time unit
otherwise the process Q will start.

- Timed Interrupt $P \triangle_d Q$
Unless the process P is finished until d , it is terminated and
the process Q will follow, but P is finished within d , Q will not be invoked to
start

Timed CSP Explorer

- A program described in ML (Meta Language)
- Lexical analysis, parsing of Timed CSP Processes described in CSP_M and generation of ML functions
- Execution of the ML functions
- Refinement analysis (timed trace/time-wise trace) for safety (trace based) verification



Implementation of CSP processes with ML (1)

- Definition of additional ML datatypes
 - `datatype process`
`= Proc of (event -> process) | Stop | Skip | Bleep ;`
 - process has 4 constructors
 - Proc is a function to take an event as argument and return a process
 - `datatype event`
`= Event of string*chanType ;`
 - event as a tuple of (string, chanType)
 - Time information for Timed CSP processes will be added afterwards
 - `datatype chanType`
`= Int of int | Seq of int list | String of string`
`| Any | None ;`

Implementation of CSP processes with ML (2)

- Example of a CSP Operator ; Event Prefix $a \longrightarrow P$

```
prefix(Event(ch,v),P:process)=  
let  
  fun temp(Event(ch',v')) if ch=ch' andalso v=v' then P else Bleep  
in  
  Proc temp  
end
```

- Execution of processes ;

$$P = b \longrightarrow (a \longrightarrow SKIP)$$

- execution of the process with single step

```
fun run(Proc temp)  
= temp;
```

```
-  
- val P= prefix(Event("b",None),prefix(Event("a",None),Skip)) ;  
val P = Proc (fn,[Event (#,#)]) : process  
- val P1=run(P) ;  
b  
val P1 = fn : event -> process  
- val P2=run(P1(Event("b",None))) ;  
a  
val P2 = fn : event -> process  
- val P3=run(P2(Event("a",None))) ;  
tick.  
val P3 = fn : event -> process  
-  
- □
```

Extension for Timed CSP

- Addition of Time constructor to datatype event
datatype event
= Event of string*chanType | **Time of int** ;
- Modification of ML functions for CSP operators extended by time concept
- Implementation of Timed CSP operators
 - fun tprefix(Event(ch,v), Time d, P:process)
 - fun timeout(P:process, Time d, Q:process)
 - fun tinterrupt(P:process, Time d, Q:process)

Execution of Timed CSP processes (1)

- Process with timed interrupt

$test = out!10 \rightarrow$

$$((a \rightarrow SKIP \{a\} \parallel_{\{b\}} b \rightarrow SKIP) \Delta_{10} c \xrightarrow{5} SKIP)$$

- ML expression & execution

```

- exec(test()) ;
fun test() =
  prefix(Event("out", 10),
    concurrent(
      p a
    ),
    Time 10, b
  )
  tprefix(Event("c", 5),
    c
  )
)

```

```

event: b 10time
b
event: a 10time
a
tick
event: 10time
10time
event: c
c
event: 5time
5time
tick
*
*
*

```

```

event: 10time
10time
event: c
c
event: 5time
5time
tick
*
*
*
finished.
val it = () : unit
-

```

```

prefix(Event("b", None), Skip)

```

Execution of Timed CSP processes (2)

- Process with Timed event prefix and timeout

$$HELEN = (meet \xrightarrow{60} work \rightarrow SKIP) \triangleright^{30} work \rightarrow SKIP$$

$$CARL(d) = WAIT d \wp ((meet \xrightarrow{60} home \rightarrow SKIP) \triangleright^{45} home \rightarrow SKIP)$$

$$test = HELEN \parallel (CARL(15) \sqcap CARL(40))$$

```

ML
- use "para.ml";
[opening para.ml]
val HELEN = Proc (fn,[Event (#,#),Time 30]) : process
val CARL = fn : int -> process
val test = Proc (fn,[Event (#,#),Event (#,#),Time 30]) : process
val spec = fn : chanType -> process
val Meet = fn : chanType -> process
val it = () : unit
- exec(test);
event: L R 30time
L
event: 15time
15time
event: meet 15time
meet
event: 60time
60time
event: work home
work
event: home
home
tick
*
event: home
home
event: work
work
tick
*
*
end
val test =
share(HELEN,[Event("meet",None)], internal(CARL(15),CARL(40)))
event: 15time
15time
event: work 30time
work
event: 30time
30time
event: home
home
tick
*
event: 30time
30time
event: work home
work
event: home
home
tick
*
event: home
home
event: work
work
tick
*
*
event: R 30time
R
event: 30time
30time
event: work 10time
work
event: 10time
10time
event: 45time
45time
event: home
home
tick
*
event: home
home
event: work
work
tick
*
event: 10time
10time
event: work 45time
work
event: 45time
45time
event: home
home
tick
*
event: 45time
45time
event: work home
work
event: home
home
tick
*
event: 45time
45time
event: work home
work
event: home
home
tick
*
event: 45time
45time
event: home
home
tick
*
*
finished.
val it = () : unit
-

```

Refinement with Timed CSP Explorer

- Trace refinement (Safety verification with Timed CSP traces)

$$SPEC \sqsubseteq_T IMP \iff traces(SPEC) \supseteq traces(IMP)$$

- Trace timewise refinement

$$SPEC \sqsubseteq_{TF} IMP$$

$$\iff \forall (s, X) \in TF[IMP] \cdot \#s < \infty \Rightarrow strip(s) \in traces(SPEC)$$

- $strip(\langle (15, meet), (45, work), (45, home) \rangle) = \langle meet, work, home \rangle$

- $refine(Spec, Imp)$

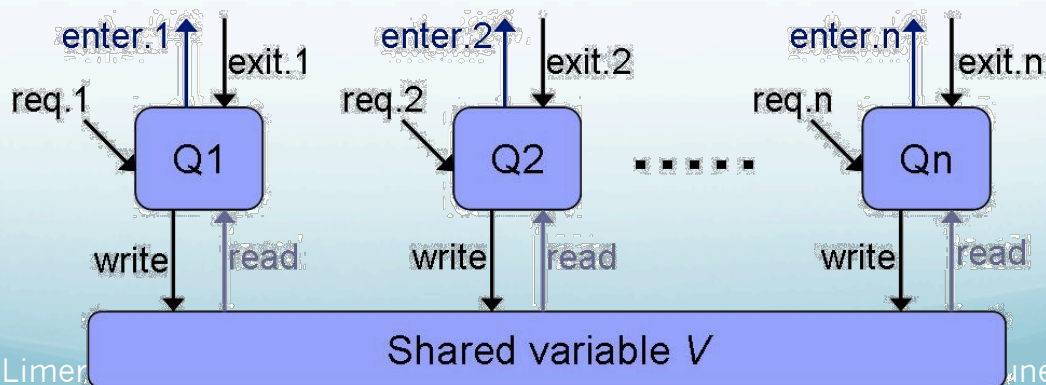
- All the traces generated by Imp process are followed with Spec
- If Spec follows them all w/o Bleep, refinement is established

Exclusive control of shared resources

- Exclusive access control for the critical region in shared resources
 - The critical region can be accessed by any number of processes but only one can access at one time
 - If a process accesses the region the other process should wait this access is over
 - We need an efficient and safe mechanism to control the processes in as each process accesses the critical region as if only one process occupies it.
- As one of candidates to be used for the exclusive control is called Fischer's algorithm
 - Idea of this example comes from S. Schneider, "Concurrent and Real-time systems The CSP Approach" (2000)

Fischer's algorithm with CSP

- $Q(i) = req.i \rightarrow read?x \rightarrow$
 if $x \neq 0$ then *SKIP*
 else $write!i \rightarrow enter.i \rightarrow exit.i \rightarrow STOP$
 - ◆ read shared memory and if it is 0, write I (process ID) and enter (occupy)
 - ◆ Independent operation
- $QS = Q(1) ||| Q(2) ||| \dots ||| Q(n)$
- $V(value) = (write?x \rightarrow V(x)) \square (read!value \rightarrow V(value))$
- $FIS = QS [| | read, write | |] V(0)$
 - ◆ V value must be initially zero
- Specification: $enter.i$ must be followed with $exit.i$ before $enter.i'$



Refinement of Fischer's algorithm

- Trace verification with Timed CSP explorer for this algorithm with $n=2$

- as a Specification for this algorithm,

$$SPEC = (enter.1 \rightarrow exit.1 \rightarrow SPEC \square enter.2 \rightarrow exit.2 \rightarrow SPEC)$$

- and hided the events *read*, *req*, *write* from *FIS*

$$FIS = FIS \setminus \{| read, write, req |\}$$

- Refinement result: observation of *enter.1* & *enter.2* in a trace

```
event: L R
L
event: (read).0 N
(read).0
event: (write).2 N
(write).2
event: (write).1
(write).1
event: enter.1 enter.2
enter.1
event: exit.1 enter.2
exit.1
stop
event: enter.2
enter.2

not satisfy
(req).1 (req).2 (read).0 L (read).0 (write).2 (write).1 enter.1 enter.2
val it = () : unit
```


Extension of Fischer's algorithm with Timed CSP

- Redefinition of process $Q(i)$ with Timed CSP

$$Q(i) = req.i \rightarrow read?x \rightarrow$$
$$\quad \text{if } x \neq 0 \text{ then } SKIP$$
$$\quad \text{else (} write!i \xrightarrow{\epsilon} read?y \rightarrow$$
$$\quad \quad \text{if } y \neq i \text{ then } SKIP$$
$$\quad \quad \text{else } enter.i \rightarrow exit.i \rightarrow SKIP) \triangleright^{\delta} STOP$$

- Introduction of waiting time ϵ for writing i into the shared memory
- Introduction of maximum time limit for occupation of the shared memory δ
- $\epsilon > \delta$ should be satisfied
 - In this analysis, we have modified also *SPEC, FIS* slightly

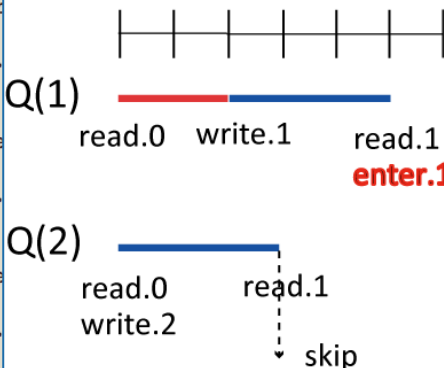
Refinement of the extended Fischer's algorithm

- Trace timewise refinement with Timed CSP Explorer
 - $\epsilon = 4, \delta = 2$
 - $\epsilon = 2, \delta = 4$

```

read.0
event: write.1 2time
write.1
event: 4time
4time
event: read.1
read.1
event: enter.1
enter.1
event: exit.1
exit.1
stop
*
*
*
event: 2time
2time
*
*
*
Succeeded
*
*
satisfy
val it = () : unit
- □
    
```

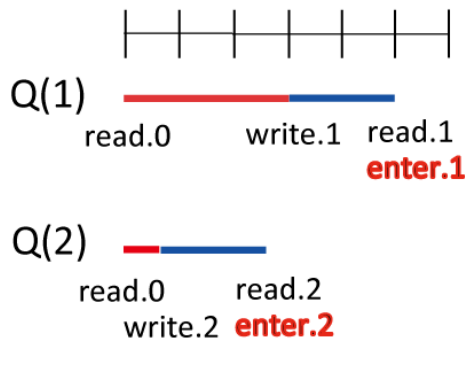
$\epsilon > \delta$



Q(1) read.0 write.1 read.1
enter.1

Q(2) read.0 write.2 read.1
skip

$\epsilon < \delta$



Q(1) read.0 write.1 read.1
enter.1

Q(2) read.0 read.2
enter.2

```

2time
event: read.
read.2
event: enter.
enter.2
event: exit.
exit.2
stop
event: write.
write.1
event: exit.
exit.2
stop
event: 2time
2time
event: exit.
exit.2
stop
event: read.1
read.1
event: enter.1 exit.2
enter.1
here2:
not satisfy
req.1 req.2 read.0 L read.0 write.2 2time read.2 enter.2 write.1 2time read.1 enter.1
val it = () : unit
- □
    
```

Failed

Summary and Outlook

- We have developed (are developing) a verification tool for Timed CSP processes, but it has just started a year ago out of our urgent necessity
- Timed CSP Explorer makes a lexical analysis and parsing of a machine readable (CSP_M) description of a Timed CSP process, and generates the corresponding ML expression
- run, exec command of the tool can generate trace sequences that the process will produce (step by step or continuously till end)
- refine command can verify the process with its specification in terms of trace and trace timewise refinement
- Development is still underway
 - We need more efficient, complete and robust parsing system
 - and must add failures based (failure timewise and timed failure) refinement facility